

## Teacher Resource Book

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## The Primary Maths series

## What is Primary Maths?

Primary Maths is a unique new series that provides teachers with a complete and comprehensive mathematics teaching and learning program for students in years F to 6. This detailed Teacher Resource Book contains the program and acts as a foundation for the busy teacher.

The Primary Maths series at each year level includes:

- the Teacher Resource Book
- a full-colour Student Activity Book
- a Practice \& Homework Book (except for the Foundation level).


## Why was Primary Maths developed?

The Primary Maths series offers a range of stimulating and challenging activities for all strands, including Number and algebra, Statistics and probability, and Measurement and geometry.

The philosophy upon which Primary Maths is based is the idea that students learn most effectively through physical and mental activities related to experiences in their world. The series breathes life into the mathematics curriculum by providing experiences that introduce and consolidate fundamental knowledge, skills and understanding.

Primary Maths is designed as a carefully sequenced program to support teachers in delivering quality mathematics experiences to students. With a suggested teaching sequence and detailed learning activities, it offers teachers full and continuous support.

Ideas on how to introduce and reflect on each lesson, tasks to support learners along the sequence, teaching tips and additional blackline masters and assessment pages are provided.

## What do the different components of Primary Maths provide?

The Primary Maths Teacher Resource Book is the foundation of the series. It contains a yearly program, structured in 36 units of work, and includes weekly plans for teaching and learning, activities linked to assessment, teaching notes, half-yearly and yearly assessments, and blackline master pages.


The Primary Maths Student Activity Book is filled with relevant, graded activities to motivate learners. Fullcolour photos and illustrations link teaching and learning activities to everyday contexts and help to bring the maths curriculum alive. Arranged in strands and substrands, the pages allow for flexibility and for students to build on prior knowledge.


The Primary Maths Practice \& Homework Book contains 36 double-page units of work that complement the Primary Maths Student Activity Book. It can be used for homework or to provide extra practice in the classroom.


Primary Maths includes links to relevant Cambridge HOTmaths lessons and activities at years 3 to 6 . Cambridge HOTmaths is a comprehensive mathematics learning system - an interactive online maths learning, teaching and assessment resource for students and teachers. Visit the Cambridge HOTmaths website for more information:
www.cambridge.edu.au/hotmaths
Primary Maths has also been conveniently referenced to Cambridge Maths-in-a-Box, a hands-on teaching resource that brings numeracy alive in the classroom. Each stage of Maths-in-a-Box contains 175 full-colour cards that provide additional support and enrichment for a complete classroom program.


## How do I use Primary Maths?

The Primary Maths Teacher Resource Book is designed to support teachers in delivering a comprehensive mathematics program. Opportunities have been taken to link learning across the substrands where appropriate.

The Teacher Resource Book contains a suggested sequence for learning, along with detailed lesson notes. The program includes ideas to introduce and reflect on each lesson and tasks to support learners along the sequence, including additional blackline masters and assessment pages.


The Primary Maths Student Activity Book is filled with interesting activities to motivate learners. Graded activities are presented using photos and illustrations that link to the real world and create interest. Discussion ideas, information boxes and challenge questions ensure that the book caters to students of all aptitudes.


The Primary Maths Practice \& Homework Book nicely complements the Primary Maths Student Activity Book. It provides extra classroom practice and/or homework activities. There are four sections for each of the 36 units, including real-world problems, quick mental questions, revision of prior learning and practice of new concepts. The units closely follow the teaching sequence set out in the Teacher Resource Book.


We encourage you to take possession of this program and use it as relevant to the needs of your students and yourself. You may use as much or as little of the wealth of information and ideas presented in this Teacher Resource Book as you like.

Ed Lewis and Jim Grant
Consultants

## Introduction

Primary Maths is an all-new series of print and digital resources written especially for the years F to 6 Australian Curriculum: Mathematics. It provides an authoritative and practical interpretation of the new content strands, content descriptors, elaborations and achievement standards, building on learning sequences and teaching methods that have been shown to work in the state curricula. Primary Maths provides a range of mathematics activities that encourage students to think about situations and problems, to talk to others about their ideas and to develop their own strategies as confident learners.

Mindful that the Australian Curriculum specifies minimum content to be covered, the series includes some topics that are necessary prerequisites for specified content. It also includes logical extensions in a range of topics. The result is a reliable teaching structure and sequence that can be taught confidently with the minimum of preparation. All activities, explanations and exercises have been designed to cater for the full range of ability levels.

Along with the three content strands (Number and Algebra, Measurement and Geometry, and Statistics and Probability), the four proficiency stands are clearly listed and defined within the Primary Maths Teacher Resource Book. Although some topics or lessons may lend themselves more closely to one particular proficiency strand, all of the strands play a role in good teaching and learning.

While the proficiency strands are interwoven and interdependent, clearly defining four separate strands helps us to think about what resources we might use in our classes. Creating a lesson plan or set of exercises that take students along all four strands may take a little thought, but should be simple to put into practice.

As a class teacher, it is worthwhile considering how your lesson plan addresses each of the four proficiency strands. The four proficiency strands are:

## Understanding

Students build a robust knowledge of adaptable and transferable mathematical concepts. They make connections between related concepts and progressively apply the familiar to develop new ideas. They develop an understanding of the relationship between the 'why' and the 'how' of mathematics. Students build understanding when they connect related ideas, when they represent concepts in different ways, when they identify commonalities and differences between aspects of content, when they describe their thinking mathematically and when they interpret mathematical information.

At year 2, Understanding includes connecting number calculations with counting sequences, partitioning and combining numbers flexibly, and identifying and describing the relationship between addition and subtraction and between multiplication and division.

The appearance of this icon U in the Teacher Resource Book indicates that the Understanding proficiency strand is addressed by the activity adjacent to it.

## Fluency

Students develop skills in choosing appropriate procedures; carrying out procedures flexibly, accurately, efficiently and appropriately; and recalling factual knowledge and concepts readily. Students are fluent when they calculate answers efficiently, when they recognise robust ways of answering questions, when they choose appropriate methods and approximations, when they recall definitions and regularly use facts, and when they can manipulate expressions and equations to find solutions.

At year 2, Fluency includes counting numbers in sequences readily, using units iteratively to compare measurements, listing possible outcomes of chance events, and describing and comparing time durations.

The appearance of this icon F in the Teacher Resource Book indicates that the Fluency proficiency strand is addressed by the activity adjacent to it.
Problem Solving
Students develop the ability to make choices; interpret, formulate, model and investigate problem situations; and communicate solutions effectively. Students formulate and solve problems when they use mathematics to represent unfamiliar or meaningful situations, when they design investigations and plan their approaches, when they apply their existing strategies to seek solutions, and when they verify that their answers are reasonable.

At year 2, Problem Solving includes formulating problems from authentic situations, making models and using number sentences that represent problem situations, planning routes on maps, and matching transformations with their original shape.

The appearance of this icon PS in the Teacher Resource Book indicates that the Problem Solving proficiency strand is addressed by the activity adjacent to it.
Reasoning
Students develop an increasingly sophisticated capacity for logical thought and actions, such as analysing, proving, evaluating, explaining, inferring, justifying and generalising. Students are reasoning mathematically when they explain their thinking, when they deduce and justify strategies used and conclusions reached, when they adapt the known to the unknown, when they transfer learning from one context to another, when they prove that something is true or false, and when they compare and contrast related ideas and explain their choices.

At year 2, Reasoning includes using known facts to derive strategies for unfamiliar calculations, comparing and contrasting related models of operations, describing connections between 2D and 3D representations, and creating and interpreting simple representations of data.

The appearance of this icon $B$ in the Teacher Resource Book indicates that the Reasoning proficiency strand is addressed by the activity adjacent to it.
The essential foundations of the Primary Maths series are:

- The interconnectedness of the components within each of the three content strands are emphasised and grouped into units of work that can be taught comfortably within a school year.
- All exercises classify questions according to the four proficiency strands of the Australian Curriculum, enabling teachers to easily offer a range of questions that emphasise different proficiencies. As well as the core understanding and fluency skills, much attention has been paid to problem-solving and reasoning questions to promote students' logical and analytical thought processes, enabling them to employ creative mathematical strategies in a wide range of contexts and to achieve a deeper understanding.


## Teaching sequence

## Year 2

## Term 1

| Unit I | Unit 2 | Unit 3 |
| :---: | :---: | :---: |
| Number and Place Value ACMNA027 | Addition and Subtraction ACMNA029 ACMNA030 | Area ACMMG037 |
| - Represent and order numbers up to 300 <br> - Count forwards and backwards by ones <br> - Indentify the number before and after a given number | - Use and explain strategies for solving addition and subtraction problems <br> - Use counting on as a strategy for solving addition problems <br> - Use counting back as a strategy for solving subtraction problems <br> - Use doubles and near doubles as a strategy for addition | - Compare and order several shapes and objects based on area using appropriate uniform informal units <br> - Compare and order two or more areas using informal units <br> - Record area by referring to the number and type of units used <br> - Draw the spatial structure of repeated units |
| Unit 4 | Unit 5 | Unit 6 |
| Shape ACMMG043 | Shape ACMMG042 | Time <br> ACMMG040 ACMMG04I |
| - Describe the features of threedimensional objects <br> - Name, describe, sort and model cubes, cones, cylinders, spheres and prisms <br> - Recognise three-dimensional objects in pictures and the environment and presented in different orientations <br> - Indentify two-dimensional shapes as faces of three-dimensional objects | - Describe and draw two-dimensional shapes with and without digital technologies <br> - Indentify key features of squares, rectangles, triangles, kites, rhombuses, circles, hexagons and trapeziums <br> - Count edges and corners of 2D shapes | - Name and order months and seasons <br> - Use a calendar to identify the date and determine the number of days in each month <br> - Use calendars to locate specific information such as finding a given date and saying what day it is <br> - Identify personal or culturally specific days |
| Unit 7 | Unit 8 | Unit 9 |
| Multiplication and Division ACMNA03I | Chance ACMSP047 | Patterns and Algebra ACMNA035 ACMNA036 |
| - Represent multiplication as groups and arrays <br> - Describe equal rows and solve problems involving equal rows <br> - Recognise multiplication as repeated addition | - Indentify practical activities and everyday events that involve chance <br> - Describe outcomes as 'likely' or 'unlikely' <br> - Identify some events as 'certain' or 'impossible' <br> - Classify a list of everyday events according to how likely they are to happen, using the language of chance | - Continue number patterns involving skip counting <br> - Represent number patterns on a number line <br> - Build addition facts to at least I2 <br> - Relate addition and subtraction facts |

## Year 2

## Term 2

| Unit IO | Unit II | Unit 12 |
| :---: | :---: | :---: |
| Number and Place Value ACMNA027 | Volume and Capacity ACMMG037 | Addition and Subtraction ACMNA029 ACMNA030 |
| - Apply an understanding of place value to represent and order numbers <br> - Count forwards and backwards by ones <br> - Indentify the number before and after a given number | - Use appropriate informal units to estimate, measure and record volume and capacity <br> - Compare and order the capacities of two or more containers and the volumes of two or more models or objects <br> - Packs cubic units into rectangular containers so there are no gaps | - Use and explain strategies for solving addition and subtraction problems <br> - Use a hundreds chart to assist with addition and subtraction <br> - Use 'building to ten' as a strategy for solving addition problems |
| Unit I3 | Unit 14 | Unit I5 |
| Location ACMMG044 | Multiplication and Division ACMNA031 ACMNA032 | Fractions and Decimals ACMNA033 |
| - Interpret simple maps of familiar locations and identify relative positions of key features <br> - Describe the position of objects in models, photographs and drawings <br> - Describe the path from one location to another on a drawing <br> - Use drawings to represent the position of objects along a path <br> - Construct arrangements of objects from a set of directions | - Represent multiplication as repeated addition <br> - Represent division as grouping into equal sets | - Model and describe halves and quarters of a shape <br> - Model and describe halves and quarters of a collection |
| Unit 16 | Unit I7 | Unit 18 |
| Length ACMMG037 | Data ACMSP049 ACMSP050 | Area ACMMG037 |
| - Compare and order several shapes and objects based on length using appropriate uniform informal units <br> - Recognise the need for a formal unit to measure lengths or distances <br> - Compare lengths using finger length, counters, hand spans or a piece of string | - Collect, check and classify data <br> - Interpret information presented in a table <br> - Recognise the usefulness of tally marks <br> - Organise data into a simple column graph and interpret results <br> - Identify categories of data and use them to sort data | - Compare and order several shapes and objects based on area using appropriate uniform informal units <br> - Use appropriate informal units to estimate and measure area <br> - Draw the spatial structure (grid) of the repeated units <br> - Describe why the area remains constant when units are rearranged <br> - Record area by referring to the number and type of units used |

## Year 2

## Term 3

| Unit 19 | Unit 20 | Unit 21 |
| :---: | :---: | :---: |
| Number and Place Value ACMNA027 | Mass ACMMG038 | Addition and Subtraction ACMNA029 ACMNA030 |
| - Apply an understanding of place value to represent and order numbers <br> - Count forwards and backwards by ones <br> - Indentify the number before and after a given number | - Compare masses of objects using balance scales <br> - Compare and order the masses of two or more objects using informal units <br> - Use an equal arm balance to find two collections of objects that have the same mass <br> - Calculate differences in mass by measuring and comparing | - Use and explain strategies for solving addition and subtraction problems <br> - Represent addition on a number line <br> - Add two 2-digit numbers using trading <br> - Make generalisations involving addition |
| Unit 22 | Unit 23 | Unit 24 |
| Shape ACMMG043 | Addition and Subtraction ACMNA029 ACMNA030 ACMNA034 | Multiplication and Division ACMNA03I |
| - Describe the features of threedimensional objects <br> - Identify geometric features such as the number of faces, corners or edges <br> - Identify two-dimensional shapes as faces of three-dimensional objects <br> - Recognise that objects look different from different views <br> - Represent three-dimensional objects by making models and drawings | - Use and explain strategies for solving addition and subtraction problems <br> - Subtract a one-digit number from a two-digit number with trading <br> - Count collections of coins <br> - Indentify equivalent values in collections of coins | - Represent multiplication as repeated addition <br> - Label collections of equal rows and equal groups using words and symbols <br> - Model the commutative property of multiplication |
| Unit 25 | Unit 26 | Unit 27 |
| Fractions and Decimals ACMNA033 | Volume and Capacity ACMMG037 | Location ACMMG044 |
| - Model and describe halves, quarters and eighths of a whole shape <br> - Model and describe halves, quarters and eighths of a collection | - Compare and order several shapes and objects based on volume and capacity using appropriate uniform informal units <br> - Use appropriate informal units to estimate, measure and record volume and capacity <br> - Compare and order the capacities of two or more objects by marking the change in water level when each is submerged <br> - Compare capacities using a range of containers | - Interpret simple maps of familiar locations and identify relative positions of key features <br> - Describe the position of objects in models from memory, photographs and drawings <br> - Make simple models from memory, photographs, drawing or descriptions <br> - Describe the path from one location to another on a drawing <br> - Understand that we use representations of objects and their positions, such as maps, to allow us to receive and give directions and to describe place |

Year 2
Term 4

| Unit 28 | Unit 29 | Unit 30 |
| :---: | :---: | :---: |
| Number and Place Value ACMNA026 ACMNA027 | Addition and Subtraction ACMNA030 ACMNA034 | Length ACMMG037 |
| - Investigate number sequences <br> - Recognise, model, represent and order numbers to 1000 <br> - Use the terms 'more than' and 'less than' to compare numbers <br> - Indentify missing elements in number patterns | - Subtract a two-digit number from a two-digit number with trading <br> - Perform simple calculations with money <br> - Make generalisations involving addition and subtraction | - Compare and order several shapes and objects based on length using appropriate uniform informal units <br> - Recognise the need for a formal unit to measure lengths/distances <br> - Uses the metre as a unit to measure lengths/distances <br> - Measures lengths or metres to the nearest metre or half-metre |
| Unit 31 | Unit 32 | Unit 33 |
| Transformation ACMMG045 ACMMG046 | Time ACMMG039 | Financial Maths ACMNA030 ACMNA034 |
| - Investigate the effect of one-step slides and flips with and without digital technologies <br> - Understand that objects can be moved but changing position does not alter an object's size or features <br> - Identify and describe half and quarter turns <br> - Predict and reproduce a pattern based around half and quarter turns of a shape and sketching the next element in the pattern | - Tell time to the quarter hour using the language of 'past' and 'to' <br> - Describe the characteristics of half past and quarter past times on an analogue clock | - Use and explain strategies for solving addition and subtraction problems <br> - Uses the equals sign to record equivalent number relationships <br> - Count and order small collections of Australian coins and notes according to their value |
| Unit 34 | Unit 35 | Unit 36 |
| Multiplication and Division ACMNA03I ACMNA032 | Shape ACMMG042 | Data ACMSP048 ACMSP049 ACMSP050 |
| - Model and use strategies for multiplication and division <br> - Use repeated addition or repeated subtraction as a strategy to solve problems <br> - Recognise the symbols for multiplication and division | - Describe and draw two-dimensional shapes with or without digital technologies <br> - Identify and name parallel, vertical and horizontal lines in pictures and the environment <br> - Identify key features of twodimensional shapes such as straight, vertical, parallel or horizontal lines | - Create displays of data, using lists, tables and picture graphs, and interpret them <br> - Identify a question based on one categorical variable; gather data relevant to the question <br> - Organise data into a simple column graph and interpret results <br> - Create picture graphs to represent data using one-to-one correspondence |

